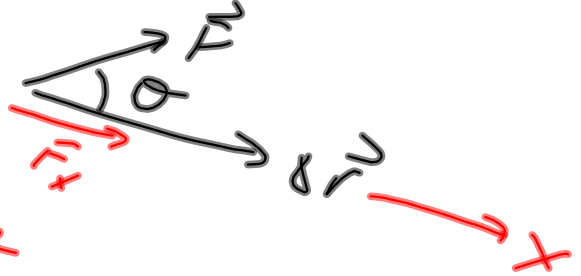


C6 $W \doteq F \Delta r \cos \theta$
 $= F_x \Delta X$



$$= \begin{cases} + & \text{acute} \\ 0 & \perp \\ - & \text{obtuse} \end{cases}$$

$$\rho = \frac{W}{\Delta t}$$

$$\epsilon = \frac{W_{out}}{W_{in}}$$

$$\text{or } \frac{W_{out}}{Q_{in}}$$

$y \uparrow$

$$W_{grav} = -mg \Delta y \quad \left. \begin{array}{l} \text{conservative} \\ \text{force} \end{array} \right\}$$

$$W_{fric} = -f \Delta X \quad \left. \begin{array}{l} \text{non-} \\ \text{conservative} \\ \text{"lossy"} \end{array} \right\}$$

$$\begin{aligned} g &= 9.8 \text{ m/s}^2 \\ &= 9.8 \text{ N/kg} \\ &9.79330\dots \end{aligned}$$

Energy Conservation -

$$E_{\text{before}} = E_{\text{after}}$$

$$\textcircled{W_{\text{net}}} \stackrel{\text{net}}{=} F_{\text{net}} \Delta X = \left(\begin{matrix} \mathbf{F} + \mathbf{F}_f + \mathbf{F}_{\text{air}} + \mathbf{F}_N + \dots \\ \mathbf{g} + \mathbf{F}_{\text{spring}} + \mathbf{F}_i \end{matrix} \right) \Delta X$$

$$\begin{aligned} & m a_x \Delta X \\ \stackrel{\text{constant}}{=} & m \left(\frac{v^2 - v_0^2}{2} \right) \end{aligned}$$

Recall constant

$$v^2 = v_0^2 + 2a \Delta X$$

$$\frac{v^2 - v_0^2}{2} = \frac{2a \Delta X}{2}$$

$$\stackrel{\text{with}}{=} \frac{1}{2} m v^2 - \frac{1}{2} m v_0^2 \stackrel{\text{net}}{=} K - K_0$$

$$W_{\text{net}} \stackrel{\text{net}}{=} \Delta K \quad \sim \text{holistic} \quad \sim \text{Work Energy Thm}$$

$$F_{\text{net}} = m a \quad \sim \text{moment by moment}$$


$$K \text{ of rollercoast car} = \frac{1}{2} (500 \text{ kg}) \left(36 \frac{\text{m}}{\text{s}} \right)^2 = 343 \text{ kJ}$$

$$80 \frac{\text{mi}}{\text{hr}} \left(\frac{1609 \text{ m}}{1 \text{ mi}} \right) \left(\frac{1 \text{ hr}}{3600 \text{ s}} \right) = 36 \frac{\text{m}}{\text{s}}$$

$$\left(\frac{\text{kg}}{\text{s}^2} \right) \text{m}^2 = \text{Nm} = \text{J}$$

$$K \text{ of ball} = \frac{1}{2} (.6 \text{ kg}) \left(15 \frac{\text{m}}{\text{s}} \right)^2 = 68 \text{ J}$$

$$K \text{ H.B.} = \frac{1}{2} (86 \text{ kg}) \left(11 \frac{\text{m}}{\text{s}} \right)^2 = 5200 \text{ J}$$

$$W_{\text{net}} = \Delta K = 0 - 5200 \text{ J} = -5.2 \text{ kJ}$$

$$\Rightarrow F(1 \text{ m})(-1) \Rightarrow F = 5200 \text{ N} = 1200 \text{ lb}$$

$$W_{\text{spring}} = F(1.5 \text{ m}) = \Delta K = 68 \text{ J} - 0$$

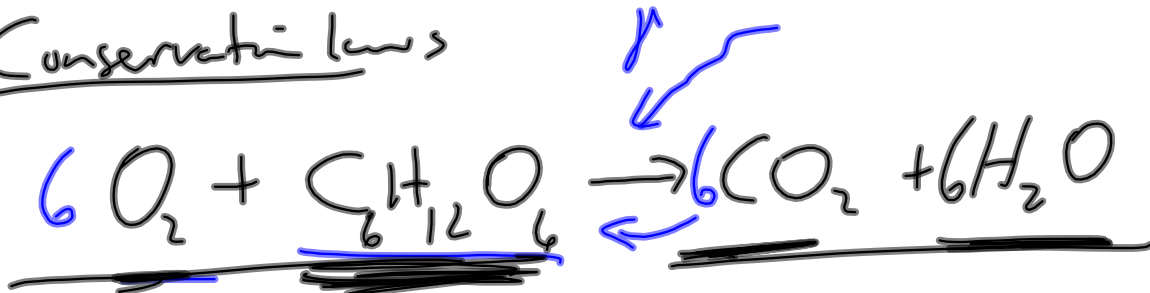
$$F = \frac{68 \text{ J}}{1.5 \text{ m}} = 45 \text{ N} \sim 10 \text{ lb}$$

$f_{air} \ll mg$
 $V_A = 0$
 $K_A = 0$
 $K_B = \frac{1}{2} m V_B^2$
 $= \Delta K$
 $W_{net} = W_g + W_T + W_f$
 $= -mgy$
 $mgR = \frac{1}{2} m V_B^2$
 $V_B = \sqrt{2gR}$
 $\approx 4.09 \text{ m/s}$

x	i: B → C	y
$a_x = 0$	$a_y = -g \sim \text{const.}$	
$v_x = v_{x0} + a_x t$	$v_y = v_{y0} + a_y t$	
$\Delta x = v_{x0} t + \frac{1}{2} a_x t^2$	$\Delta y = v_{y0} t + \frac{1}{2} a_y t^2$	
$\Delta x = v_B \sqrt{\frac{2H}{g}}$	$= -H$	
	$\frac{2H}{g} = \frac{1}{2} \frac{t^2}{g} \Rightarrow t = \sqrt{\frac{2H}{g}}$	

$\Delta x = v_B \sqrt{\frac{2H}{g}}$
 $= \sqrt{2gR} \sqrt{\frac{2H}{g}}$
 $= \sqrt{4RH}$
 $= \sqrt{4(0.855 \text{ m})(1.00 \text{ m})}$
 $= 1.910 \text{ m}$

Conservation laws



$$\# \text{ of } C = \# \text{ of } C$$

$$\# \text{ of } O = \# \text{ of } O$$

mass of reactants = mass of prod.

$$E = \underline{K} + U_g + U_s$$

$$= \frac{1}{2}mv^2 + \underline{mgy} + \frac{1}{2}kx^2$$

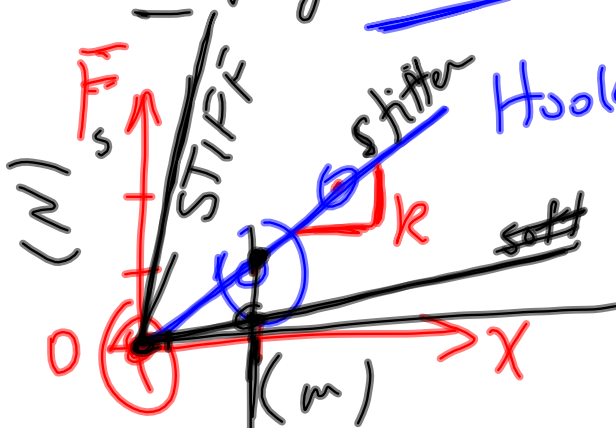


$\vec{F}_{net} = m\vec{a} \sim$ moment by moment

$W_{net} = \Delta K \quad K = \frac{1}{2}mv^2 \quad \underline{W} = \underline{F} \Delta \underline{x}$

$W_{net} = W_g + W_s + \underbrace{W_T + W_F + W_N + \dots}$

$= -mg\Delta y - \frac{1}{2}kx^2 + W_{nc}$ non-conservative



Hooke's Law spring

$\underline{y} = \underline{m}\underline{x} + \underline{b}$

$F_s = kx$

$F_{spring} = 9.21 x$
 $(N) = \left(\frac{N}{m}\right)(m)$

$k \sim$ stiffness coefficient

$W_{spring} = \vec{F}_x \Delta x \cos \theta = \left(0 + \frac{kx}{2}\right) x \cos 180^\circ = -\frac{1}{2}kx^2$

$$\boxed{W_{\text{net}} = \Delta K} \quad \sim \text{NZL} \quad y \uparrow$$

$$= \underbrace{W_g}_{\text{gravity}} + \underbrace{W_s}_{\text{spring}} + W_{\text{nc}}$$

$$W_{\text{nc}} = \Delta K - W_g - W_s$$

$$= \underbrace{\Delta K}_{\text{kinetic}} + \underbrace{\Delta U_g}_{\text{grav. pot.}} + \underbrace{\Delta U_s}_{\text{spring pot.}}$$

$$W_{\text{nc}} = \underbrace{(K + U_g + U_s)_f}_{\text{final energy}} - \underbrace{(K + U_g + U_s)_i}_{\text{initial energy}}$$

$$W_{\text{nc}} = E_f - E_i = \Delta E$$

$$\boxed{W_{\text{nc}} = \Delta E}$$

\sim energy conserved
 (if $W_{\text{nc}} = 0$)

$K = \frac{1}{2}mv^2$
 $U_g = mgy$
 $U_s = \frac{1}{2}kx^2$

y_1 y_2 y_3

$A \rightarrow B$ $v=0$

$E_1 = K + U_g + U_s$
 $= \frac{1}{2}mv^2 + mgy + \frac{1}{2}kx^2$
 $= 0 + mgR + 0$

$E_2 = K + U_g + U_s$
 $= \frac{1}{2}mv^2 + mg(0) + 0$

$W_{nc} = W_f + W_{air}$
 $A \rightarrow B = 0 + 0$
 $\Rightarrow \Delta E = 0$

your spring
 $F = kx$
 $v = 0$

later,
 after
 mass
 dropped

kx
 x
 mg
 v

Note: b/c

y pts up
 & x pts dn
 & $x=0=y$
 @ origin
 $y = -x$

!:- string holding mass in place, burn it to release

$$E = K + U_g + U_s$$

$$= \frac{1}{2} m v^2 + mgy + \frac{1}{2} kx^2$$

$$= \frac{1}{2} m v^2 - mgx + \frac{1}{2} kx^2$$

@ release
 $v=0, y=0,$
 $x=0$
 so
 $E=0$

$W_{nc} = 0$ b/c friction f is the only other force and it's tiny.

$0 = \frac{1}{2} m v^2 - mgx + \frac{1}{2} kx^2$ describes all subsequent motion

Now you can ask where ($x=?$) is it stopped ($v=0$)?

$$0 = 0 - mgx + \frac{1}{2} kx^2$$

$$\Rightarrow 0 = \frac{1}{2} kx^2 - mgx$$

$$0 = x \left(\frac{1}{2} kx - mg \right)$$

$\hookrightarrow \dots$

Recall basic algebra, when $0 = A \cdot B$, either $A=0$ or $B=0$